

## Lagrangian FE model for bottle manufacturing simulation

#### Pavel Ryzhakov, M.-A. Celigueta

Centre Internacional de Mètodes Numèrics en Enginyeria (CIMNE)



### CIMNE

The International Center for Numerical Methods in Engineering (**CIMNE**) is a research organization created in 1987 at the heart of Technical University of Catalonia (UPC) as a partnership between the Government of Catalonia and UPC, in coop. with UNESCO.

The aim of CIMNE is the development of <u>numerical methods</u> and computational techniques for advancing knowledge and technology in engineering and applied sciences.

CIMNE employs some 250 scientists and engineers who work in the different offices of CIMNE around the world. CIMNE has also established a network of 30 Classrooms in partnership with Universities in Spain and 11 Latin American countries.





Over its history, CIMNE has taken part in over 2,000 RTD projects in cooperation with some 500 companies, universities and research centers worldwide.



### **KRATOS** Multiphysics

Kratos is designed as an Open-Source HPC framework for the implementation of numerical methods for the solution of engineering problems. It is written in C++ and is designed to allow collaborative development by large teams of researchers focusing on modularity as well as on performance.

Kratos Team is a continuously growing community with its current core located in CIMNE, Barcelona. It also has branches in Germany, UK, Russia, Iran and China.



#### **KRATOS Multiphysics team**







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### Outline

- 1. Motivation and objectives
- 2. Technological context
- 3. Numerical model
- 4. Algorithmic issues
- 5. Examples
- 6. Challenges and open questions
- 6. Conclusions

#### 1.1 Motivation

Bottle manufacturing is a billions-euro industry world-wide

– Beverages, fragnances, containers...



Competition: optimization necessary



Technological procedure: mainly based on crammanship and experience

#### **Questions to answer:**

- How can the container weight be reduced without compromising on its strength?
- How to design the parison mould in the best way?
- What is the optimal air pressure at different stages?
- What would different cooling conditions lead to?

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### 1.2 Objectives

- Develop a <u>robust and efficient</u> tool for bottle manufacturing simulations.
- The tool must be developed <u>in</u> <u>axisymmetric</u> and in <u>3D</u> (many containers are not axissymmetric, thermal conditions are often not axis-symmetric even for bottles with circular cross-sections)
- Predict <u>wall thickness</u>, temperature and stress distributions



### 1.3 Challenges

- Strongly temperature-dependent properties
- Moving surfaces and interfaces
- Necessity of good precision on relatively rough meshes to obtain solution in reasonable time
- Contact modeling
- "Validation" problems:
- Absence of well-defined benchmarks (mostly conference papes, the few journal articles present simulation realizations, not providing the data necessary for reproducing the simulation)

#### State-of-the-art

#### Scientific community:

Eulerian+Level Set:

C.G. Giannopapa et al: Modeling the blow-blow forming process in glass container manufacturing. *Journal of Fluids Engineering, 2011.* 

Lagrangian formulation, const. viscosity, no thermal model

- (Feulvarch et al.: 3D simulation of glass forming process, *J. Mat. Processing technology*, 2005)
- Lagrangian axis-symmetric formulation, thermally coupled: J.M.A. Cesar de Sa: "Numerical modelling of glass forming processes", *Eng. Computations*

#### Commercial:

Specific: NoGrid (meshless method in 3D (Finite Pointset Method)

General purpose: **ABAQUS** (Eulerian formulation+Level Set)

Problem: no well-established benchmark. No reference data! Multiple conference papers, very few journal articles



# 2. Technological context: bottle manufacturing stages









#### Material properties: commercial silicate glass



Visco-elastic material, however at forming temperature range **viscous** approximation is acceptable

Viscocity changes from 140^E06 Pa.s to 400 Pa.s between 700°C and 1200°C

Glass density (almost constant): 2438 kg/m3 at 700C - and 2367 kg/m3 at 1100 °C

**Specic heat** almost **constant** (1400-1420 J/kg\*K)

**Diffusivity** changes from 0.0000015 m2/s at 700 C to 0.0000065 m2/s at 1100 C.

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### 3. Numerical model

- Viscous incompressible fluid
- Thermally-coupled
- Air is neglected (only glass+mould or wall)

Important features:

Moving boundariesChanging properties

PFEM-like Lagrangian strategy—

Advantageous paradigm for convecting properties

#### What is PFEM?

The **PFEM** is a numerical method that uses a Finite Element mesh to discretize the physical domain and to integrate the differential governing equations.

In **PFEM** the nodes of the mesh move according to the equations of motion in a Lagrangian fashion. The <u>nodes transport their momentum together with all</u> <u>their physical properties</u> thus behaving as particles.

At the end of each time step the mesh has to be rebuild as the nodes have been moved to their new time step position.



#### What is PFEM?

Main **PFEM** features are:

- FEM mesh + properties stored at nodes
- Moving mesh (Lagrangian formulation)
- Re-meshing (Delaunay)
- External boundary identification (using the alphashape technique + boundary markers)

PFEM for glass forming simulation?

#### PFEM + ? = **PGLASS**

#### **PFEM steps**





### Governing equations

$$\begin{split} \rho \frac{\partial \mathbf{v}}{\partial t} + \nabla p - \nabla \cdot \left( 2 \mu \epsilon(\mathbf{v}) \right) &= \rho \mathbf{g} \\ \nabla \cdot \mathbf{v} &= 0 \end{split}$$

$$\rho c \frac{\partial T}{\partial t} = k \nabla^2 T + Q$$

No-slip condition at the contact  $\mathbf{v} = \mathbf{0}$  with the mould

Inlet air pressure: Neumann b.c.  $\mathbf{t}_p = p_a \mathbf{n}$ 

Dirichlet condition at the bottle neck:  $T=T_d$ 

Glass-air interaction is not considered

Mould thermal conditions?





#### Axisymmetric model



**Navier-Stokes equations** 

$$\rho \frac{D \mathbf{v}_a}{Dt} + \nabla p_a - \nabla \cdot (2\mu \dot{\epsilon}_a(\mathbf{v}_a)) = \rho \mathbf{g}_a$$
$$\nabla \cdot \mathbf{v}_a = \mathbf{0}$$
$$\mathbf{v}_a = \begin{bmatrix} \mathbf{v}_r(r, z) & \mathbf{v}_z(r, z) \end{bmatrix}^{\mathrm{T}}$$

**Strain vector** 

$$p_a = p(r, z)$$

$$\dot{\epsilon}_{a} = \begin{pmatrix} \dot{\epsilon}_{r} \\ \dot{\epsilon}_{z} \\ \dot{\epsilon}_{\theta} \\ \dot{\gamma}rz \end{pmatrix} = \begin{pmatrix} \frac{\partial \mathbf{v}_{r}}{\partial r} \\ \frac{\partial \mathbf{v}_{z}}{\partial z} \\ \frac{\mathbf{v}_{r}}{r} \\ \frac{\partial \mathbf{v}_{r}}{\partial z} + \frac{\partial \mathbf{v}_{z}}{\partial r} \end{pmatrix}$$

# FEM-descritization and numerical algorithm

Mechanical

 $\begin{pmatrix} \frac{\mathbf{M}}{\Delta t} + \mu \mathbf{L} & \mathbf{G} \\ \mathbf{D} & \tau \mathbf{L} \end{pmatrix} \begin{pmatrix} d\bar{\mathbf{v}} \\ d\bar{p} \end{pmatrix} = \begin{pmatrix} \bar{\mathbf{r}}_m \\ \bar{\mathbf{r}}_c \end{pmatrix}$  Exactly a state of the second state of the

Modified fractional step split

Excellent effficiecy and mass conservation

Staggered solution: mechanicalthermal equations

Thermal

$$\mathbf{M}\frac{T_{n+1}-T_n}{\Delta t} - k\mathbf{L}T_{n+1} = \mathbf{Q}$$

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 $log_{10}\mu = A + \frac{B}{T - T_0}$ Fulcher equation Improving mass conservation in simulation of incompressible flows. Ryzhakov P. et al Int. Jour. for Num.Methds. in Eng., 2012. An algorithm for the simulation of thermally coupled low speed flow problems: P. Ryzhakov, R. Rossi, E. Oñate, Int. Jour. Num. Meth. in Fluids, 2012.

### Algorithmic issues

## Boundary preserving refinement, boundary markers



(a) Mesh deterioration



(b) Mesh-preserving refinement

Identify the boundaries with boundary markers. Ensure that no "holes" are created: subdivide stretched edges/faces maintaining mesh resolution



### Algorithmic issues

Pre-matured contact must be avoided Otherwise an error in bottle wall thickness will be of order *h*. (unacceptable, since the final wall thickness is descretized with several elemets only, otherwise meshes will count millions of elements).



#### Contact detection





(a) Glass and wall are separated





(b) Fictitious contact elements are created



(c) Removal of interface nodes close to the wall (d) Stick contact between the glass and the wall



#### 5. Examples

#### Validation example: TV panel pressing



C.Berndhauser. Tc25 - modelling of glass forming processes short review of activities 2000 - 2009. In *GlassTrend - ICG seminar and workshop INNO-VATION IN GLASS PRODUCTION*. International Comission on Glass, 2013.





t=0 s-t=0.25 s t=0.5 s

t=0.75 s t=1 s

t=1 25

12

-t=3 s

9

### ANSYS, TNO, NoGrid



C.Berndhauser. Tc25 - modelling of glass forming processes short review of activities 2000 - 2009. In GlassTrend - ICG seminar and workshop INNO-VATION IN GLASS PRODUCTION. International Comission on Glass, 2013.



#### **Present Lagrangian model**







#### **Benchmark proposal**

#### **Gravity stretch+final blow**

Assumed iinitial temperature distribution

Real material properties, Simplified thermal model (prescribed temperature at mould walls)

1158.4 1110.2

1061.9 1013.6

965.36 917.09 868.82

820.54 772.27 724



"SEKT bottle VP4679" (data: no industrial secret, data provided by Dr. J. Jimenez Vidrio&Eng. COMM)

#### Gravity stretch + Final blow

Thermo-mechanical simulation







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#### Interface elements close-up

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#### Premature blow

Premature pressure application

(must be applied once the glass reached the mould wall at the bottom)



#### Bottle shape



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### Thickness distribution. Axisymmetric simulation









#### Axisymmetric - 3D comparison (soins60 bottle, geometry provided by *Ramon Clemente*)



#### Axisymmetric - 3D comparison

SOINS60 flask (parison)







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#### What is the use?

Parison mould design (trials on the computer instead of the real factory)



### Summary and conclusions

- **PFEM** was adapted to suit the problem of interest Efficient modified fractional step method was implemented for solving the governing equations Control over the error in thickness **Excellent mass conservation** Benchmark example elaborated Computational times - hours (3D), minutes (axisymmetric)
- 3D axisymmetric validated



### Challenges

- Missing data... Precise <u>viscosity</u> maps in the glass (or even approximated ones) must be obtained from <u>direct temperature measurements</u> performed in multiple location.
- Incorporation of the mould in the thermal computations? (very large increment in comp. cost)
- Ad-hoc thermal model: heat sink at the mould surface – experimental data necessary



#### Future work

- Graphical User Interface
- Incorporation of thermal data in the ad-hoc model – under development (thermal data missing)
- Comparison with experiments carried by IQS and Ramon Clemente
- Improve efficieny: apply Jacobian-independent time integration strategy (XIVAS)
- Coupling of the two steps (counter and final

Sergio Rodolfo Idelsohn, Norberto Marcelo Nigro, Juan Marcelo Gimenez, Riccardo Rossi, and Julio Marcelo Marti. A fast and accurate method to solve the incompressible Navier-Stokes equations. *Engineering Computations*, 30(2):197–222, 2013.



### Acknowledgements

This research is being partially supported by Ramon Clemente glass and by **COMETAD** project of the National RTD Plan of the Spanish *Ministerio de Economía y Competitividad* (ref. MAT2014-60435-C2-1-R)



### Thank you for your attention!



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